# A Countermeasure Against Statistical Ineffective Fault Analysis

Jakub Breier, Mustafa Khairallah, Xiaolu Hou and Yang Liu

Abstract—When considering practical attacks against cryptographic implementations, Fault Injection Attacks (FIA) pose a powerful tool that can recover the secret key within few encryptions. Over the past few decades they have become a wellstudied topic both by academic an industry practitioners.

Current state-of-the-art countermeasures against Fault Injection Attacks (FIA) provide good protection against analysis methods that require the differences in the correct and faulty ciphertext to derive the secret information, such as Differential Fault Analysis (DFA) or collision fault analysis. However, recent progress in Ineffective Fault Analysis (IFA) and Statistical IFA (SIFA) constitutes a real threat against cryptographic implementations. Such methods cannot be thwarted by standard FIA countermeasures that focus on detecting the change in the intermediate data.

In this paper, we present a novel method based on error correcting codes that protects implementations against SIFA. We design a set of universal error-correcting gates that can be used for block cipher implementations. We analyze a hardware implementation of protected GIFT-64 and show that our method provides 100% protection against SIFA.

Index Terms—fault injection attacks, ineffective fault analysis, countermeasures, error-correcting codes, SIFA

# I. INTRODUCTION

In the era of Internet-of-Things, people interact with small inexpensive low-power devices on a daily basis. These devices are often easily accessible, and to keep the costs down, without comprehensive protection against sophisticated adversaries. One class of such adversarial models are *physical attacks* that exploit the physical characteristics of the device to derive the secret information, often in a form of a cryptographic key. These are further divided into *side-channel attacks* that passively observe the device, and *fault injection attacks* that actively tamper with the device.

Fault injection attacks have become a powerful tool for implementation attacks against cryptography [1]. Many different fault analysis methods have been proposed up to date, so the attacker can choose based on her capabilities and the target cipher implementation. Recently, several powerful proposals utilizing Statistical Ineffective Fault Analysis (SIFA) have been introduced [2]–[4]. SIFA can be either executed by injecting stuck-at fault in the intermediate value during the execution of an algorithm or by exploiting the bias that can be observed by faulting inputs of logic gates. Based on

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observing the statistical bias in the ciphertext, the attacker can gain information of the attacked intermediate value and eventually get the secret key. As stuck-at fault is considered to be a stronger adversarial model, in the rest of this paper we will focus on preventing against it. Such prevention work for the other model in the same manner. The main strength of (S)IFA lies in the ineffectiveness of standard fault injection countermeasures to thwart the attack. Normally, the implementation-level prevention techniques aim at detecting value changes in the computation to raise an alarm. This can be done by using a redundant computation circuits, various codebased techniques, of infective countermeasures that "infect" the entire cipher state after fault to hide the information leakage from the fault. However, in case of (S)IFA, the attacker exploits the knowledge whether the computation was correct or not - she does not need to check the difference between the faulty and correct ciphertext. The key guess then can be made based on the knowledge of the correct ciphertext and the bias of the fault value in the intermediate state. And therefore, raising an alarm from the countermeasure is enough for the attacker to determine the value she wants to discover.

As mentioned in [4], to prevent from these attacks, it is advised to utilize sensitive-enough physical sensors, e.g. ring oscillator based [5], that detect the physical disturbances of the circuit no matter whether the value has changed or not. However, since the sensor is not a part of the cryptographic circuit, there is always a possibility to unplug it or make it ineffective. For that reason, it is better to have multiple layers of protection, both on the circuit and the implementation level.

**Our contribution.** In this paper, we propose a countermeasure against (S)IFA that utilizes error-correcting codes. The main idea is to prevent the attacker from knowing whether the fault occured or not. We provide a set of universal error-correcting gates that can be used for implementing linear and non-linear operations of block ciphers. Our results show 100% fault coverage against the considered attacker model. Additionally, any type of side-channel protection can be implemented over our SIFA countermeasure.

**Organization.** The rest of this paper is organized as follows. Section II presents the related work in this field. Section III provides the theoretical background for our method. Application of the method to ciphers is described in Section IV, followed by evaluation in Section V. Discussion is provided in Section VI, and finally, Section VII concludes this work.

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# II. RELATED WORK

In this part, we provide the necessary background on ineffective fault attacks, statistical fault attacks, and their combination. Later, we give an overview of countermeasures against fault attacks.

## A. Ineffective Fault Attacks

Ineffective Fault Attacks (IFA) were originally proposed by Clavier in 2007 [6]. This fault analysis method exploits type of fault which changes a variable to a particular value – and in case the variable already holds this value, no change can be observed. As an example, let us assume we have a one bit variable x which is secret. This variable is being processed in a device we have previously profiled and we can assume with a high probability that we are capable of changing a certain bit in a data unit to "1" with a well-aimed fault injection. Now, we process x with our device, launch the fault injection, and observe the output. In case we see a difference at the output, it means the original value of x was "0." Otherwise, if there is no observable change at the output, we can assume with a high probability that the original value of x was "1."

# B. Statistical Fault Attacks

Statistical Fault Attacks (SFA), introduced by Fuhr et al. [7] exploit the situation when the attacker is able to change an intermediate value to a biased value by injecting a fault. Three fault models were presented: 1) stuck-at-0; 2) stuck-at-0 with probability of 0.5 or logical AND with random uniform value with probability 0.5; 3) logical AND with random uniform value. The authors showed how the method works on AES, where the recovery of 4 bytes of the secret key took between 6-80 faulty ciphertexts, depending on the used model.

# C. Statistical Ineffective Fault Attacks

Statistical Ineffective Fault Attacks (SIFA) [4] are an intersection between IFA and SFA.

In [2]–[4] authors experimentally used ineffective faults to break cryptosystems without the need of the deeper analysis of the cipher, which is normally necessary for using other methods, such as Differential Fault Analysis.

# D. Fault Attack Countermeasures

Fault attack countermeasures mostly focus on preventing fault models that aim at altering the values during the execution, e.g. differential fault analysis. They either try to detect the change or prevent the attacker from getting information from the faulty output. On the other hand, in case of (S)IFA, the information whether there was a change during the computation is sufficient to get some information about the internal state. Currently, only device-level countermeasures can be used for preventing (S)IFA, such as sensors or special packages. However, the cipher implementer has normally no control over these countermeasures and a specialized device needs to be used to provide them. For further overview of different countermeasures, we refer the interested reader to [8].

# III. METHODS

In this part, we first detail the necessary background on coding theory, followed by the idea of using codes against (S)IFA. Later, we describe ways to implement our countermeasure with an example on binary AND operation.

#### A. Coding theory background

A binary code, which we denote by C, is a subset of  $\mathbb{F}_2^n$ , the *n*-dimensional vector space over  $\mathbb{F}_2$ , where *n* is called the *length* of the code C. Each element  $c \in C$  is called a *codeword* of C and each element  $x \in \mathbb{F}_2^n$  is called a *word* [9, p.6]. Take two words  $x, y \in \mathbb{F}_2^n$ , the Hamming distance between x and y, denoted by dis (x, y), is defined to be the number of places at which x and y differ [9, p.9]. More precisely, if  $x = x_1 x_2 \dots x_n$  and  $y = y_1 y_2 \dots y_n$ , then

$$\operatorname{dis}\left(\boldsymbol{x},\boldsymbol{y}\right) = \sum_{i=1}^{n} \operatorname{dis}\left(x_{i}, y_{i}\right),$$

where  $x_i$  and  $y_i$  are treated as binary words of length 1 and hence

$$\operatorname{dis}\left(x_{i}, y_{i}\right) = \begin{cases} 1 & \text{if } x_{i} \neq y_{i} \\ 0 & \text{if } x_{i} = y_{i} \end{cases}$$

Furthermore, for a word  $x \in \mathbb{F}_2^n$ , the *Hamming weight* of x, HW(x) := dis(x, 0) [9, p.46]. For a binary code C, the *(minimum) distance* of C, denoted by dis(C), is [9, p.11]

$$\operatorname{dis}\left(\mathcal{C}\right) = \min\{\operatorname{dis}\left(\boldsymbol{c},\boldsymbol{c}'\right):\boldsymbol{c},\boldsymbol{c}'\in\mathcal{C},\boldsymbol{c}\neq\boldsymbol{c}'\}.$$

Definition 1: [9, p.39] In case C is a subspace of  $\mathbb{F}_2^n$ , C is called a linear code. A linear code with dimension k, length n and minimum distance d is called an [n, k, d]-binary code.

Definition 2: [9, p.13] Let v be a positive integer. C is v-error-correcting if minimum distance decoding with incomplete decoding rule is applied, v or fewer errors can be corrected.

Remark 1: C is v-error correcting if and only if dis  $(C) \ge 2v + 1$  [9, p.13].

Considering the (S)IFA, as we are mostly dealing with 1- and 2-bit faults, the distance for the used codes should be at least 3 and 5, respectively.

#### B. Our Countermeasure Idea

Normally, it would be of no use for the attacker to affect high number of bits at the same time, since the probability of the original variable to have the exact value that is being injected gets lower with each stuck-at faulty bit. Therefore, it is safe to assume that practical attacks would aim at changing 1 or at most 2 bits of the variable.

The main idea of our countermeasure is to make the attacker unsure whether there was a change to the variable or not. For this purpose, we propose usage of error correcting codes that were thoroughly evaluated against fault injection in [10]. The working principle of the (S)IFA protection is depicted in Figure 1. The error correction ensures that in case the fault was injected, the variable will regain its original value. Therefore,



Fig. 1. Error correction against IFA when attacking the same bit position in two different codewords - 11110000 and 00001111. In case of set to "1" fault: (a) original value changes after fault and later is corrected back, (b) original value does not change after fault.

the attacker is not able to distinguish whether the change due to the fault occured or not.

The crucial parameter of the code in this case is the distance d, which specifies how many bits we allow the attacker to target. To allow v bits to be targeted, we need distance to be at least 2v+1 to be able to correct the codeword to the original value [9].

# C. Implementation Options

In general, there are two ways to implement encoding based countermeasures: either in a table look-up form where the address navigation is done by using codewords [10]; or by computing the operations on the codewords directly, while performing integrity checks after predefined number of operations [11]. In our work we focus on the second approach due to the fact that it is faster and has lower memory consumption.

# D. Example

Let us consider a simple binary AND operation, taking two single bits as inputs and one single bit as output. To correct one bit, distance between codewords needs to be at least 3. We can construct a truth table for an implementation of errorcorrecting AND gate (implementation details of the gate are explained in the next section), stated in Table I, where the encoding is as follows:  $0 \mapsto 000$  and  $1 \mapsto 111$ . Columns correspond to the first operand and rows correspond to the second operand. We can see that the table entries contain only two values, depending on the distance between the input word and the two codewords. That also means that even if both input values get faulted, the correction will still work. It is important to note that this particular example might leak sidechannel information, since in case the Hamming weight (HW) of the word is  $\leq 1$ , it corrects to 000, and if the HW is  $\geq 2$ , it corrects to 111.

# **IV. APPLICATION TO CIPHERS**

In this section we describe a low-cost hardware implementation of our countermeasure. We use the lightweight SPN ciphers Skinny-128-128 [12] and GIFT-64-128 [13] as

TABLE I TRUTH TABLE FOR ERROR-CORRECTING AND GATE, USING A LINEAR CODE WITH TWO CODEWORDS:  $0 \mapsto 000; 1 \mapsto 111.$ 

&	000	001	010	011	100	101	110	111
000	000	000	000	000	000	000	000	000
001	000	000	000	000	000	000	000	000
010	000	000	000	000	000	000	000	000
011	000	000	000	111	000	111	111	111
100	000	000	000	000	000	000	000	000
101	000	000	000	111	000	111	111	111
110	000	000	000	111	000	111	111	111
111	000	000	000	111	000	111	111	111

examples. Additionally, we outline a protection method for 2-bit faults.

#### A. Single-Bit Faults

First, we consider the [3,1,3]-binary code (3-Repetition Hamming code) stated in Section III-D. To reduce the cost, we use the fact that this code is a linear code. Hence, XOR/XNOR/Inversion operations can be performed on the codewords simply by applying the corresponding Boolean operations in a bitwise manner. This approach allows us to reduce the cost of implementing linear operations of the ciphers. However, this also means that the faults will propagate linearly through the gates. We assume that the correction will only be performed in the non-linear (Sbox) Layer. We study a fault model where each codeword has at most 1 faulty bit at the input of each round.

Based on the previous rationale, we can define a set of gates that are used to operate on the codewords:

$$\begin{aligned} RNOT &: \{z_2, z_1, z_0\} = \{x_2 \oplus 1, x_1 \oplus 1, x_0 \oplus 1\} \\ RXOR &: \{z_2, z_1, z_0\} = \{x_2 \oplus y_2, x_1 \oplus y_1, x_0 \oplus y_0\} \\ CAND &: \{z_2, z_1, z_0\} = \{(x_2x_1 \lor x_1x_0 \lor x_0x_2) \\ \land (y_2y_1 \lor y_1y_0 \lor y_0y_2), (x_2x_1 \lor x_1x_0 \lor x_0x_2) \\ \land (y_2y_1 \lor y_1y_0 \lor y_0y_2), (x_2x_1 \lor x_1x_0 \lor x_0x_2) \\ \land (y_2y_1 \lor y_1y_0 \lor y_0y_2)\} \\ COR &: \{z_2, z_1, z_0\} = \{(x_2x_1 \lor x_1x_0 \lor x_0x_2) \\ \lor (y_2y_1 \lor y_1y_0 \lor y_0y_2), (x_2x_1 \lor x_1x_0 \lor x_0x_2) \\ \lor (y_2y_1 \lor y_1y_0 \lor y_0y_2), (x_2x_1 \lor x_1x_0 \lor x_0x_2) \\ \lor (y_2y_1 \lor y_1y_0 \lor y_0y_2), (x_2x_1 \lor x_1x_0 \lor x_0x_2) \\ \lor (y_2y_1 \lor y_1y_0 \lor y_0y_2)\} \end{aligned}$$

The circuit diagrams are depicted in Figure 2. As mentioned earlier, both the NOT and XOR gates have no effect on the fault value. The AND/OR gates have to be implemented at least 3 times independently to make sure that if the adversary injects a fault in one of the instances, it does not propagate to the other two bits.

Given this set of gates, we study the implementation of the GIFT cipher's Sbox, proposed in [13]. We chose the software-optimized implementation of the Sbox as a reference as it has lower number of NOT/XNOR/NAND/NOR gates, making it more suitable for our gate set. This implementation requires 5X+1N+3A+1R, where X, N, A, R stands





Fig. 2. Adjusted gates to operate on codewords (a,b), and error-correcting gates (c,d).

for XOR, NOT, AND and OR gates, respectively. Overall, one round of GIFT-64 needs 16 Sboxes and 32 XORs for key addition, 112X+16N+48A+16R. Using our gate set instead, we can implement the GIFT-64 round using 336X+48N+1728A+624R. We estimate the overall cost compared to the unprotected implementation of GIFT-64 as follows: X=2.25GE, N=0.7GE, A=R=1.2GE. We also need to take into consideration that we have to store the state, which requires 64 Flip-Flops for the unprotected case and 192 Flip-Flops for the protected case. Hence, the countermeasure requires 6× area overhead for ASIC. For FPGA, we can reduce such cost to only 3×, since the CAND and COR gates can take advantage of the 6-to-1 Look Up Table structures in the modern FPGA, such that each of them can be implemented using only 3 LUTs.

Similarly, we study the implementation of the members of the Skinny family of tweakable block ciphers. They use two different Sboxes, one is a 4-bit Sbox and the other is an 8-bit Sbox. The 4-bit Sbox requires 4X+4R+4N, while the 8 bit Sbox requires 8X+8R+8N. Moreover, Skinny also uses two different diffusion layers, depending on the block size. The Round Constants require 6X+1N, while the Key addition requires either 32X or 64X. Finally, the MixColumn operation requires either 64X or 128X. Overall, if the block size is 64 bits, one round requires 166X+65N+64R. If the block size is 128 bits, it requires 326X+129N+128R. For the protected case, we need 498X+195N+2112R and 978X+387N+4224R, respectively. Hence, we estimate the overhead for ASIC to be around  $5.6 \times$ , which is slightly lower compared to GIFT-64. This is because Skinny has higher X/(A+R) ratio, i.e. the ratio between linear components and non-linear components is higher, due to the MixColumn operation, as opposed to the bit permutation in GIFT.

## B. Double-Bit Faults

Our countermeasure can be extended to double-bit faults by using [5,1,5]-binary code instead. In this case the cost for the RNOT and RXOR gates is multiplied by 5, while CAND and COR gates can be implemented using 123A+54R and 120A+57R, respectively. Hence, the overall cost of the implementation of GIFT-64 is 560X+80N+7824A+3504R, in addition to 320 Flip-Flops for the state storage. In case of ASIC, we estimate the overhead to be  $\approx 25\times$ . While the cost might seem relatively high, given that SIFA is one of the strongest attacks on cipher implementations, we believe such cost can be justified for sensitive applications that require high security.

# V. EVALUATION

We have analyzed the ineffective fault analysis conditions of the GIFT Sbox implementation proposed in Section IV-A. We have constructed a digital logic circuit analysis tool that loops through all the possible inputs, injects a stuck-at fault at every single gate in the circuit, and checks the output for errors. We have utilized a single fault adversarial model which is the most common model used in the literature. The assumption on correcting capabilities of our proposal is that in case there is a fault that propagates through the Sbox layer, it will either be corrected at the following Sbox layer (in case of inner rounds) or at the final decoding stage. Therefore, to simulate this behavior, we have analyzed two different scenarios:

1) first/middle round fault, followed by another round;

2) last round fault, followed by an error correcting decoder. These two scenarios are depicted in Figure 3.

As it would be computationally impractical to analyze the full GIFT state, we took advantage the properties of the permutation layer that divides the state into four 16-bit substates. We analyzed one 16-bit sub-state, which shows the



Fig. 3. Two evaluation scenarios: (a) fault is injected in the middle round and (b) fault is injected in the last round. Round where the fault is injected is indicated by red color, while the round/block where the fault is corrected is indicated by green color.

 TABLE II

 Results on simulating ineffective fault analysis against the gates proposed in Section IV. Description of each scenario is given in Figure 3.

		Correct	outputs	Faulty outputs		
Gate	#	Scenario 1	Scenario 2	Scenario 1	Scenario 2	
AND	660	100%	100%	0%	0%	
OR	396	100%	100%	0%	0%	
XOR	276	100%	100%	0%	0%	
CAND	28	100%	100%	0%	0%	
COR	4	100%	100%	0%	0%	
RXOR	30	100%	100%	0%	0%	
RNOT	4	100%	100%	0%	0%	

behavior of the entire state. That means, for each gate we analyzed  $2^{16}$  inputs for stuck-at-0 and stuck-at-1 fault. We tried to fault every bit of each input. That means, for example in case of AND gates, the total number of experiments was 660 gates  $\times 2^{16}$  input values  $\times 2$  fault models  $\times 2$  inputs = 173,015,040, for each scenario.

The results are stated in Table II. Simulation time for different types of gates varied between 30 seconds (COR/RNOT gate) and 1.5 hours (AND gate) for Java-based implementation of the simulator. As can be seen, the circuit analysis utilizes the error-correcting properties of the linear code as described in Section III. Every ineffective fault was captured either in the subsequent round in case of Scenario 1, or in the final decoder in case of Scenario 2. This shows that the implementation following our proposal is robust against (S)IFA that utilizes 1-bit faults.

# VI. DISCUSSION

In this part we first provide discussion on different type of code that can be used – a Hamming-(7,4) code. Then, we discuss what happens if a fault is injected into encoding/decoding circuit. Later, we give an idea on how to implement the encoding protection in software, followed by discussion on how error-correcting codes work against differential fault analysis. We close this section by discussing how to combine our method with side-channel protection techniques.

# A. Hamming-(7,4) Code

Cheaper codes can be used to get cheaper implementations, such as the Hamming-(7,4) code, which encodes 4-bit nibbles into 7-bit codewords. This code can correct all single bit faults, as well. In this scenario, the 4-bit Sbox can be implemented as an equivalent 7-bit look-up table. Since the overall encoded state is smaller, the cost of the linear parts of the circuit is lower. However, the attacker can have more targeted attacks that aim at internal states of the Sbox. In such case the analysis of how such faults will propagate to the output of the Sbox is not clear. In other words, the attacker may be able to inject a fault in an internal gate that generates codewords with multiple faulty bits.

# B. Faulting Encoding/Decoding Circuit

As one may have noticed, we did not consider faults into the encoding/decoding circuits that surround the cipher implementation. We will explain this in the following.

In case of the *encoding* circuit, if there is a fault in the input, it will change the value of the codeword to another codeword, effectively changing the plaintext input to the cipher. That means, the attacker would get the same situation as in case of differential cryptanalysis – she would have to cryptanalyze the entire cipher. If there is a fault in the output of the encoding circuit, the error-correcting gates in the first round will correct it the same way as in the middle of the cipher.

In case of the *decoding circuit*, the attacker would be effectively faulting the resulting ciphertext. That would not give her any additional information on either the plaintext nor the secret key.

# C. Software Implementation

Fault injection countermeasures without side-channel protection can increase the leakage coming from side channels [14]. Therefore, whenever a fault countermeasure is implemented, and there is a risk of an adversary capable of mounting a side-channel attack, it is necessary to consider adding a side-channel protection. There are generally two approaches to this - either implementing a universal countermeasure that protects against both types of attacks, or implementing two different protection methods. [10] proposed a code-based countermeasure following the first approach by extending [15], where they constructed codes that provide protection for different leakage models. While the speed overhead of such implementation is reasonable - 82.5% for PRESENT-80 implementation from [16], the memory requirements are relatively high. For example, in case of 8-bit architectures, one binary look-up table takes 65 kB [16].

The second approach can be useful in case one of the countermeasures is already implemented at the hardware level, but the other one has to be added additionally. This is a case in many industrial applications, where a secure co-processor handles and guarantees certain level of protection, and the software library takes care of the rest. As our method uses error-correcting gates to deploy fault resistant functionality, it is easy to implement side-channel countermeasure of choice on top of that, either in hardware or software.

# D. Differential Fault Analysis

A thorough analysis of error-correcting encoding scheme w.r.t. DFA was given in [10]. The work shows that it is necessary to match the assumed attacker strength with the used code. More specifically, the code distance always needs to be twice as long as the attacker's capabilities to flip certain number of bits, otherwise there is a possibility to correct one codeword into another by flipping enough bits.

# E. Side-Channel Protection

Fault injection countermeasures without side-channel protection can enhance the leakage coming from side channels [14]. Therefore, whenever a fault countermeasure is implemented, and there is a risk of an adversary capable of mounting a side-channel attack, it is necessary to consider adding a side-channel protection. There are generally two approaches to this – either implementing a universal countermeasure that protects against both types of attacks, or implementing two different protection methods.

It was shown before that it is possible to construct a code with the properties that actually provide side-channel protection for different leakage models [15], [17], [18]. These schemes alone can already provide certain level of fault protection as detailed in [19]. Later, it was also shown that a code-based countermeasure can be utilized to combine the protection against both side-channel and fault injection attacks [10], [20], [21]. As we do not focus on combined protection method in this work, we would like to direct interested reader to aforementioned works.

Another approach, a combination of two countermeasures, can be useful in case one of the countermeasures is already implemented at the hardware level, but the other one has to be added additionally. This is a case in many industrial applications, where a secure co-processor handles and guarantees certain level of protection, and the software library takes care of the rest. As our method uses error-correcting gates to deploy fault resistant functionality, it is easy to implement side-channel countermeasure of choice on top of that, either in hardware or software.

#### VII. CONCLUSION

In this paper we have proposed a novel method to protect cipher implementations against ineffective fault analysis. Our work is based on error-correcting codes that can be efficiently implemented in the form of error-correcting hardware gates. Attacker capabilities can be matched by the choice of proper code, e.g. for 1-bit fault models, at least a 3-bit code needs to be used, while for 2-bit fault model, at least a 5-bit code has to be used. We have evaluated a hardware implementation of protected GIFT-64 and our results show 100% fault coverage.

In the future, it would be interesting to extend the protection against side-channel attacks by utilizing adequate codes, as was shown in [10], or by combining it with additional countermeasure, such as masking. Additionally, it would be good to look into automatic deployment of such countermeasures, as was shown in [22] for several other cases.

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