# A Note on "Three-Factor Anonymous Authentication and Key Agreement Based on Fuzzy Biological Extraction for Industrial Internet of Things"

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**Abstract**. We show that the key agreement scheme [IEEE Trans. Serv. Comput. 16(4): 3000-3013, 2023] fails to keep user anonymity, not as claimed. The scheme simply acknowledges that user anonymity is equivalent to preventing user's identity from being recovered. But the true anonymity means that the adversary cannot attribute different sessions to target users. It relates to entity-distinguishable, not just identity-revealable. To the best of our knowledge, it is the first time to clarify the explicit signification of user anonymity.

**Keywords**: Key agreement, anonymity, mutual authentication, entity-distinguishable, identity-revealable.

### 1 Introduction

Recently, Xu *et al.* [1] have presented a mutual authentication and key agreement protocol in Industrial Internet of Things (IIoT) environment. It is designed to meet many security requirements, such as mutual authentication, session key establishment, user anonymity, forward secrecy, resistance to replay attack, man-in-the-middle attack, modification attack, DoS attacks, etc.

In the proposed scenario, there are different entities including trusted authority (TA), user  $(U_k)$ , control node  $(CN_i)$ , and smart sensor device  $(SD_j)$ . The scheme consists of five phases: Initialization, Registration, Login and authentication, User join/revocation and session key update phase, Smart sensor devices join phase. TA picks a prime q to generate public parameters  $F_q, E/F_q, G, P, p$  for elliptic curve domain, where P is a base point. Set  $pr_{TA} \in Z_p^*$  as its secret key, and  $Pub_{TA} = pr_{TA} \cdot P$ as its public key. Let  $h(\cdot)$  be a hash function,  $Gen(\cdot)$  be a probabilistic generation function and  $Rep(\cdot)$ be a reproduction function of Fuzzy Extractor. The scheme can be briefly depicted as follows (see Table 1). In this note, we show that the scheme fails to keep user anonymity, not as claimed.

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	Table 1:	The Xu	et al.'s	kev	agreement	scheme
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$CN_i$	TA	$SD_j$	
$\xrightarrow{ID_{CN_i}}$ [secure channel]	Pick $pr_{CN_i}, r_{CN_i} \in \mathbb{Z}_p^*$ . Compute $Pub_{CN_i} = pr_{CN_i} \cdot P$ ,		
[secure channel] Store the parameters $RID_{CN_i}, pr_{CN_i},$	$\begin{array}{l} R_{CN_i} = r_{CN_i} \cdot P, \; RID_{CN_i} = H(ID_{CN_i} \  pr_{TA}), \\ Cert_{CN_i} = pr_{TA} + h(RID_{CN_i} \  Pub_{TA} \  Pub_{CN_i}) \cdot r_{CN_i}. \\ \\ \underbrace{\{RID_{CN_i}, pr_{CN_i}, Pub_{CN_i}, R_{CN_i}, Cert_{CN_i}\}}_{\text{Pick} \; pr_{SD_i}, r_{SD_i} \in Z_{\theta}^*. \text{ Compute} \end{array}$		
$R_{CN_i}, Cert_{CN_i}.$	$\begin{aligned} Pub_{SD_j} &= pr_{SD_j} \cdot P,  R_{SD_j} = r_{SD_j} \cdot P, \\ RID_{SD_j} &= h(ID_{SD_j} \  pr_{TA}),  Cert_{SD_j} = \\ pr_{TA} &+ h(RID_{SD_j} \  Pub_{TA} \  Pub_{CN_i} \  Pub_{SD_j}) \cdot r_{SD_j}, \\ s_{CN_i,SD_j} &= h(RID_{CN_i} \  RID_{SD_j} \  r_{CN_i} \  r_{SD_i} \  t_{SD_i}), \end{aligned}$		
Store the shared key	where $ts_{SD_j}$ is a timestamp.	Store the parameters $RID_{SD_j}$ ,	
$s_{CN_i,SD_j}$ into the memory.	$\underbrace{ \overset{s_{CN_i,SD_j}}{\longleftarrow} \overset{Pub_{SD_j},R_{SD_j},Cert_{SD_j},s_{CN_i,SD_j}}_{RID_{CN_i},RID_{SD_j},RID_{CN_i},Pr_{SD_j},} $	$pr_{SD_j}, R_{SD_j}, Cert_{SD_j}, s_{CN_i, SD_j}.$	
$CN_i$	TA	$U_k$ $ID_{U_k}$	
Store the user's pseudo identity $pid_{U_k}$ and accession number $R_{U_k}$ .	$\begin{array}{l} \mbox{Pick } r_{U_k} \in Z_p^*. \mbox{ Compute } R_{U_k} = r_{U_k} \cdot P, \\ pid_{U_k} = h(ID_{U_k} \  pr_{TA}), \\ Cert_{U_k} = r_{U_k} + h(pid_{U_k} \  R_{U_k}) \cdot pr_{TA}. \\ & \underbrace{ \begin{array}{c} (pid_{U_k}, R_{U_k}) \\ \hline \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$	Input identity $ID_{U_k}$ , password $PW_{U_k}$ . Imprint the biometric $BIO_{U_k}$ . Compute $Gen(BIO_{U_k}) = (\sigma_{U_k}, \tau_{U_k})$ , $L_{U_k} = h(ID_{U_k} \  \sigma_{U_k} \  PW_{U_k})$ . Check if $Cert_{U_k} \cdot P = R_{U_k} + h(pid_{U_k} \  R_{U_k}) \cdot Pub_{TA}$ . Pick $pr_{U_k} \in Z_p^*$ to set $Pub_{U_k} = pr_{U_k} \cdot P$ . Compute $W_{U_k} = h(Cert_{U_k} \  pid_{U_k} \  R_{U_k} \  pr_{U_k})$ . Store $pid_{U_k}, R_{U_k}, Cert_{U_k}, W_{U_k}, L_{U_k}, \tau_{U_k}$ .	
$U_k: \{pid_{U_k}, R_{U_k}, Cert_{U_k}, W_{U_k}, L_{U_k}, \tau_{U_k}\}$	$CN_i$ : { $pid_{U_k}, R_{U_k}, RID_{CN_i}, pr_{CN_i}, R_{CN_i}, Cert_{CN_i}$ }	$SD_j: \{RID_{SD_j}, pr_{SD_j}, R_{SD_j}, Cert_{SD_j}\}$	
Input $ID_{U_k}, PW_{U_k}, BIO_{U_k}$ . Compute $\sigma_{U_k} = Rep(BIO_{U_k}, \tau_{U_k})$ . Check $L_{U_k} = h(ID_{U_k}, \ \sigma_{U_k}\  PW_{U_k})$ . If so, pick the timestamp $ts_1, a \in \mathbb{Z}_p^*$ . Compute $A = a \cdot P$ , $PID_{U_k} = h(pid_{U_k}  ts_1)$ . $Auth_{U_k} = (a + Cert_{U_k}) \cdot Pub_{SD_j}$ , $Ver_{U_k} = h(ts_1  PID_{U_k}  A  R_{U_k})$ .	Check the timestamp $ts_1$ . Use $R_{U_k}$ to retrieve $pid_{U_k}$ . Check $PID_{U_k} = h(pid_{U_k}  ts_1)$ and $Ver_{U_k} = h(ts_1  PID_{U_k}  A  R_{U_k})$ . If so, compute $Auth_{CN_i} = (pr_{CN_i} + Cert_{CN_i}) \cdot Pub_{SD_j},$ $X_i = h(Auth_{CN_i}  s_{CN_i,SD_j}), Ver_{CN_i} =$	Check the timestamp $ts_2$ . Check $Ver_{CN_i} = h(PID_{U_k}   R_{U_k}   RID_{CN_i}   R_{CN_i}   A  ts_1  ts_2  X_i)$ . If so, compute $Auth'_{CN_i} = Pub_{CN_i} + Pub_{TA} + h(RID_{CN_i}   Pub_{TA}   Pub_{CN_i}) \cdot R_{CN_i} \cdot pr_{SD_j}$ .	
$\xrightarrow{M_1 = \{ts_1, PID_{U_k}, A, R_{U_k}, Ver_{U_k}\}}_{[open channel]} \rightarrow$	$h(PID_{U_k} \  R_{U_k} \  RID_{CN_i} \  R_{CN_i} \  A \  ts_1 \  ts_2 \  X_i).$	Check $X_i = h(Auth'_{CN_i}    s_{CN_i,SD_j})$ . If so, pick	
[open channel]		$b \in Z_p^*$ , compute $B = b \cdot P$ , $k_{SD_j} = b \cdot A$ ,	
Check the timestamp $ts_3$ . Check if	$\xrightarrow{M_2 = \{PID_{U_k}, R_{U_k}, RID_{CN_i}, A, ts_1, ts_2, X_i, Ver_{CN_i}\}}_{\text{[open channel]}} \rightarrow$	$Auth_{SD_j} = pr_{SD_j}(A + R_{U_k} + h(PID_{U_k}    R_{U_k}) \cdot Pub_{TA})$	
$\begin{aligned} &Ver_{SD_j} = h(B \  RID_{SD_j} \  R_{SD_j} \  t_{s3} \  Y_j). \\ &\text{If so, compute } k_{U_k} = a \cdot B, \\ &\text{su}_{k,SD_j} = h(k_{U_k} \  Auth_{U_k} \  t_{s1} \  t_{s3}), \\ &Auth_{SD_j}^{new'} = Pub_{SD_j} + Pub_{TA} + h(RID_{SD_j}). \end{aligned}$		$\begin{split} s_{U_k,SD_j} &= h(k_{SD_j} \  Auth_{SD_j} \  ts_1 \  ts_3), \\ Auth_{SD_j}^{new} &= (pr_{SD_j} + Cert_{SD_j})Pub_{U_k}, \\ Y_j &= h(Auth_{SD_j}^{new} \  s_{U_k,SD_j}), \\ Ver_{SD_j} &= h(B \  RID_{SD_j} \  R_{SD_j} \  ts_3 \  Y_j). \end{split}$	
$\ Pub_{TA}\ Pub_{CN_i}\ Pub_{SD_j}) \cdot R_{SD_j} \cdot pr_{U_k}.$	$\longleftarrow \qquad \qquad$		
Check if $Y_j = h(Auth_{SD_j}^{new'}    s_{U_k,SD_j}).$			

## 2 The signification of user anonymity

Anonymity is a security requirement adopted by many cryptographic protocols. But we find its signification is often misunderstood. We want to stress that the true user anonymity means that the adversary cannot attribute different sessions to target users. In other words, it actually relates to entity-distinguishable, not just identity-revealable. To illustrate the explicit signification of anonymity, we refer to Fig.1.

In Fig.a, the user's identity  $ID_{U_k}$  uniquely corresponds to the pseudo-identity  $pid_{U_k}$ , which uniquely corresponds to the accession number  $R_{U_k}$ . Thus, different sessions (launched by this entity) can be attributed to the entity. In this case, the unique accession number can be eventually used to recognize this entity. But in Fig.b,  $pid_{U_k}$  corresponds to different random accession numbers  $R_{U_k}^{(1)}, \dots, R_{U_k}^{(n)}$ . Therefore, the adversary cannot attribute different sessions to the entity, even though these sessions are launched by this entity.



Fig.b: The true anonymity (with different accession number  $R_{U_k}^{(i)}$ )

Figure 1: False anonymity versus true anonymity

#### 3 The loss of user anonymity

The identity of a person or thing is the characteristics that distinguish it from others. In the scheme, the user  $U_k$ 's real identity  $ID_{U_k}$  could be a regular string of some meanings, while the pseudo-identity  $pid_{U_k}$  is a random string, i.e.,

$$pid_{U_k} = h(ID_{U_k} \| pr_{TA}) \tag{1}$$

Since a real identity uniquely corresponds to a pseudo-identity (due to the collision-free property of the hash function h), one should prevent both identifiers from exposure. So, the user  $U_k$  needs to generate the session pseudo-identity

$$PID_{U_k} = h(pid_{U_k} || ts_1) \tag{2}$$

where  $ts_1$  is the current timestamp. Since the value of  $PID_{U_k}$  randomly varies in different sessions, the adversary cannot attribute different sessions to a target user. Based on this observation, the scheme is claimed to be of user anonymity (see §V, A, [1]). But we find the claim is false.

As we know, the controller node  $CN_i$  serves for a lot of users. By the received message

$$M_1 = \{ ts_1, PID_{U_k}, A, \underline{R}_{U_k}, Ver_{U_k} \}$$

$$(3)$$

which is sent via a public channel, the controller node should retrieve the target user's pseudo-identity  $pid_{U_k}$  from its local database. To do this, the node needs to use the accession number  $R_{U_k}$  to search out the long-term pseudo identity  $pid_{U_k}$ . Then compute the session pseudo identity  $PID_{U_k}$  and check its consistency.

The accession number  $R_{U_k}$  is a long-term parameter, which is issued by the trust authority in the user join phase. An accession number uniquely corresponds to a legitimate user. The adversary can obtain  $R_{U_k}$  from the captured message  $M_1$ . So, the accession number can be used to recognize the target user even though the adversary cannot use it to reveal the strings  $ID_{U_k}$  and  $pid_{U_k}$ .

To fix this flaw, one should specify a mechanism to randomly update the shared accession number  $R_{U_k}$  in each session, both for the user  $U_k$  and controller node  $CN_i$ . We refer to Ref.[2] for a possible updating mechanism, in which the shared one-time temporary identity  $tid_w$  between the sensor and controller node is randomly updated as  $tid_w^{new}$ .

By the way, the scheme also fails to keep controller node anonymity and smart device anonymity. In fact, the message

$$M_2 = \{PID_{U_k}, R_{U_k}, RID_{CN_i}, A, ts_1, ts_2, X_i, Ver_{CN_i}\}$$

contains  $RID_{CN_i}$ , where  $RID_{CN_i} = H(ID_{CN_i}||pr_{TA})$ . The adversary can use the long-term random pseudo identity  $RID_{CN_i}$  to recognize the target controller node. Likewise, the message  $M_3 = \{B, RID_{SD_j}, ts_3, Y_j, Ver_{SD_j}\}$  contains  $RID_{SD_j}$ , where  $RID_{SD_j} = h(ID_{SD_j}||pr_{TA})$  which can also be used to recognize the target smart device.

#### 4 Conclusion

We show that the Xu *et al.*'s key agreement scheme is flawed. We hope the findings in this note could be helpful for the future work on designing such key agreement schemes.

#### References

- H. Xu, et al.: Three-Factor Anonymous Authentication and Key Agreement Based on Fuzzy Biological Extraction for Industrial Internet of Things. *IEEE Trans. Serv. Comput.* 16(4): 3000-3013 (2023)
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